

# High-Order Workshop Results for Case MC1 High-Lift Common Research Model (HiLPW3)

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- ▶ Discontinuous Galerkin Finite Element Method
- ▶ Modal basis functions
- ▶ Hybrid mixed element unstructured meshes (tetrahedra, prisms, pyramids, and hexahedra)
- ▶  $p$ -enrichment and  $h$ -refinement using non-conforming elements (hanging nodes)
- ▶ Independent polynomial degree for solution and mapping basis
- ▶ Non-linear system solver: PTC Newton-Rhapson method
- ▶ Linear system solver: preconditioned flexible-GMRES (Saad 1986)
- ▶ Line implicit Jacobi, Gauss-Seidel relaxation, ILU(0)

- ▶ Compressible Navier-Stokes in conservative variables
- ▶ PDE-based Artificial Viscosity (Barter and Darmofal, Burgess)
- ▶ Spalart-Allmaras turbulence model (negative-SA variant)
- ▶ Inviscid flux: Lax-Friedrichs, Roe, AUFS
- ▶ Viscous flux: symmetric interior penalty (SIP)

# Drag and Lift Results

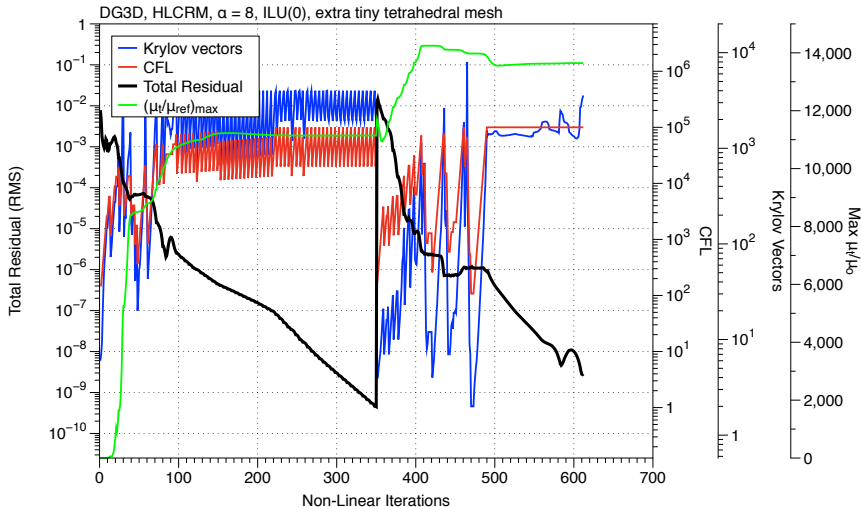
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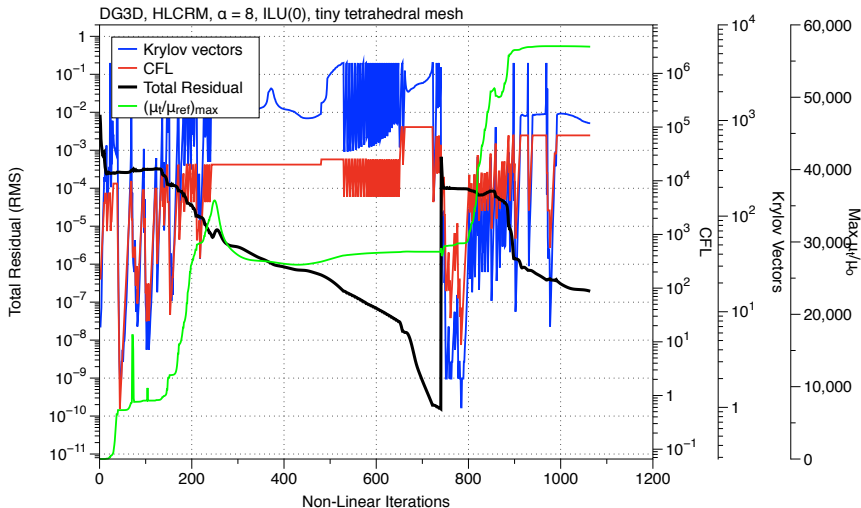
$$\alpha = 8^\circ, \text{ Roe Flux, ILU}(0)$$
$$\text{time/dof} = \frac{cputime \times procs}{\tau \times dofs}$$

case	$p$	dof $\times 10^6$	$C_L$	$C_D$	time/dof
1	1	21.6	1.7763	0.17369	1.13
2	1	70.2	1.7725	0.17314	1.60
3	2	54.1	1.7868	0.17274	0.46
4	2	175.6	1.7814	0.17253	0.28

# Residual, extra tiny mesh



# Residual, tiny mesh



# Conclusions

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- ▶ Challenging case
- ▶ Not enough runs to draw any conclusions
- ▶ Initializing  $p=2$  with  $p=1$  still difficult and time consuming
- ▶  $p=1$  tetrahedral meshes are painful for DG
- ▶ If meshing goes in direction of pure tetrahedral need to develop cell-based lines that do not rely on prisms
- ▶ ILU(0) requires a lot of memory, lines will help with this but also need matrix free high-order preconditioners